Modelling of MHD flow control for atmospheric re-entry at ONERA

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Abstract

We present recent developments in modelling magnetohydrodynamics (MHD) re-entry at ONERA. By applying a magnetic field on the re-entry ionized shocked flow, electrical currents and Lorentz forces can be generated around the vehicle. These effects can be harnessed to modify the aerodynamic forces as well as to reduce the intense heat fluxes that the vehicle experiences. We provide here an overview of the different numerical tools used for simulation of MHD phenomena occurring from high altitude to low altitude regimes. Continuum regime is in particular considered, with equilibrium or non-equilibrium effects allowed. Some applications are briefly described, from modelling laboratory MHD experiments in shock tubes to reproducing MHD-assisted re-entry in martian conditions.

1. Introduction

The use of magnetohydrodynamics (MHD) to assist vehicles as they experience the challenging environment of atmospheric re-entry has been a long-standing aspiration for space mission designers. Very early after the space age started, some authors considered to take advantage of the electric properties of the shock-generated re-entry plasma to modify the flow.¹ In particular, it was quickly realized that by applying a magnetic field on the incoming plasma, the bow shock standoff distance in front of the vehicle could be repelled away from the surface.² As a direct consequence, the thermal heat flux could be reduced providing valuable assistance to the vehicle thermal protection system. A second aspect of the MHD interaction is the generation of a reaction force acting directly on the magnetic field generation device (magnet, coils). This force adds up to the aerodynamic forces and it was suggested this could be used as a drag enhancement mechanism, especially at high altitude where atmospheric density is too small to provide useful drag: this defines the concept of MHD aero-braking.³ Past practical use of MHD-devices for re-entry has been hampered by limitations associated to the field-generation technologies. Nowadays, high-temperature compact superconducting technologies enables a new surge of interest in this promising solution.⁴

We present in this paper an overview of recent MHD-related numerical activities at ONERA. We first present the general model that we employ and the suite of numerical tools that is used to model MHD re-entry physics. We then separately treat some important aspects of the different regimes that are encountered during re-entry in the presence of an applied magnetic field. Finally, we showcase some of the applications that are currently investigated at ONERA and provide directions for future work.

2. Magnetohydrodynamics modelling

2.1 MHD model

The physics of atmospheric re-entry encompasses very different physics regimes with an accordingly broad variety of models. From the large Knudsen numbers regimes at high altitudes (≥ 60 km) to the local thermodynamic equilibrium (LTE) continuum regime at low altitudes, simulation of a full re-entry scenario remains a very challenging objective. As a result, most of numerical studies nowadays still consider the modelling of a steady-state configuration at a given condition of pressure (altitude) and velocity. This method holds as long as characteristic relaxation times of the physical processes at work are smaller than characteristic time of the re-entry trajectory. Here we consider the continuum description of the encountered flow using the classical multi-species Navier-Stokes set of equations describing the dynamics of a viscous fluid:

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DOI: 10.13009/EUCASS2023-929

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$$\frac{\partial \rho_s}{\partial t} + \nabla \cdot (\rho_s \mathbf{v}) - \nabla \cdot (\rho D_s \nabla y_s) = 0$$
⁽¹⁾

$$\frac{\partial}{\partial t}(\rho \mathbf{v}) + \nabla \cdot (p \widetilde{\mathbf{I}} + \rho \mathbf{v} \times \mathbf{v} - \widetilde{\tau}) = \mathbf{j} \times \mathbf{B}$$
⁽²⁾

$$\frac{\partial}{\partial t} \left[\rho \left(\epsilon + \frac{v^2}{2} \right) \right] + \nabla \left[\rho \mathbf{v} \left(h + \frac{v^2}{2} \right) \right] - \widetilde{\tau} \cdot \mathbf{v} - \lambda \nabla T - \nabla \cdot \left(\rho \sum_{s} h_s D_s \nabla y_s \right) = \mathbf{j} \cdot \mathbf{E}$$
(3)

Here ρ_s/ρ is the species/fluid mass density, **v** the fluid velocity, D_s the mass diffusivity of species s, y_s the mass fraction of species s, $\tilde{\tau}$ the stress tensor, p the thermal pressure, **j** the electrical current, **B** the magnetic field, ϵ the fluid internal energy, h the fluid enthalpy, λ the thermal conductivity and **E** the electric field.

As can be seen from Eq. 2 and 3, two source terms in the RHS are present with clear dependency on the electrical current **j**. The term $\mathbf{j} \times \mathbf{B}$ corresponds to the Lorentz force whereas $\mathbf{j} \cdot \mathbf{E}$ corresponds to electric field work. These quantities need to be solved alongside the classical "fluid" quantities. This can be done using electrostatic theory considering the electric field derives from an electric potential, $\mathbf{E} = -\nabla V$, and solving the charge conservation equation:

$$\nabla \cdot \mathbf{j} = 0 \tag{4}$$

which is combined with the resistive MHD Ohm's law,

$$\mathbf{j} = \boldsymbol{\sigma} (\mathbf{E} + \mathbf{v} \times \mathbf{B}) \tag{5}$$

with σ being the electrical conductivity. A Poisson-type elliptic equation on the electric potential V can then be obtained, describing the fact that no volumetric net charge creation is possible. In Ohm's law 5, the $\mathbf{v} \times \mathbf{B}$ terms describes the fact that in the conductor (here the flow) frame, the electric field is $\mathbf{E}' = \mathbf{E} + \mathbf{v} \times \mathbf{B}$ therefore in this frame we recognise the well known form of the Ohm's law $\mathbf{j} = \sigma \mathbf{E}'$. The above system of equations forms the lowmagnetic Reynolds number (R_m) version of the magnetohydrodynamics equations. In the context of re-entry MHD, the dimensionless number R_m can be found to correspond to the ratio of the induced-to-applied magnetic field. In the case of a small R_m (≤ 0.1), a situation typically assumed here, the magnetic field **B** is stationary even if allowed to be inhomogeneous. This simplifies greatly the problem with only the electric potential V to be solved. The knowledge of V allows estimation of the currents according to 5 and therefore computation of the sources terms present in Eq. 2 and 3.

2.2 Numerical strategy to model MHD re-entry

The set of equations presented in the previous section is solved by a two-code approach where the Navier-Stokes equations with MHD source terms are treated using the ONERAS CEDRE⁵ platform whereas the charge conservation equation 4 is solved using the TARANIS code also developed at ONERA.⁶ CEDRE is ONERA's multi-physics simulation HPC platform. It includes numerous physics solvers among which the finite-volume CHARME fluid solver is of particular interest for our work. It supports unstructured meshes, Euler/Navier-Stokes multi-species solvers with tabulated real gas properties capabilities. LTE or non-equilibrium chemistry reactions are supported, typically with Arrhenius-type rates. Standard scheme for spatial discretization is of MUSCL-type with explicit and implicit (e.g. GMRES) methods available for time integration of the PDEs. Additional solvers include: radiative transport (ASTRE), eulerian (SPIREE) or lagrangian (SPARTE) dispersed phase, thermal transfer in solids (ACACIA)... TARANIS is a finite-volume MHD code supporting unstructured meshes, electrostatic, magnetoquasistatic (among others) solvers with integration of widespread linear system solving library (PETSc). It includes extended MHD capabilities (Hall effet, ion slip) as well as an internal compressible fluid solver with tabulated real gas properties and a radiation transport module.

Transfers between the two codes are done using the CWIPI library.⁵ The general strategy is pictured schematically in Fig.1. At every time step, CEDRE sends to TARANIS the pressure, temperature, mass fractions and velocity distributions whereas TARANIS sends the momentum and energy source terms described in the previous section. Thermodynamical quantities received by TARANIS are used to compute the electrical conductivity whereas the velocity field is needed for computation of the $\mathbf{v} \times \mathbf{B}$ component of the Omh's law 5. In the case of an LTE gas, conductivity is deduced form tabulated values obtained using the Sethi code described in the next section. When modelling chemically non-equilibrium flows, mass fractions received by TARANIS are used alongside tabulated collisional cross sections from the LXCAT database⁷ in order to compute the conductivity.



Figure 1: Schematic of coupling between main numerical tools used for modelling MHD re-entry: CEDRE and TARA-NIS

2.3 Re-entry relevant gas properties for arbitrary mixtures: Sethi

From the previous discussion, it is clear that a central point to the numerical modelling of the atmospheric re-entry of an magnetically-assisted vehicle lies on the thermodynamical and transport properties of the encountered gas that is possibly contaminated with heat shield ablation products, whether desired or not. To address this problem, we have developed a numerical, user-friendly, python tool named Sethi. This code is able to generate tabulated thermodynamics and transport data for both the CEDRE and the TARANIS codes. It computes thermodynamical quantities from partition functions with tabulated atomic energy levels taken for example from the NIST databse.⁸ For molecular species energy levels, we follow Drellishak⁹ method to take into account coupling between electronic, rotational and vibrational energy modes. Spectroscopic tables from the literature are used to reconstruct molecular levels.¹⁰ Collective effects are somewhat introduced in the model as partition functions are truncated using the minimum value between the Fermi and Griem cutoff.¹¹ When a mixture is defined, molar fractions at a given pressure and temperature are found by using the Gibbs free energy minimization method.¹² Transport coefficients are computed according to the Chapman-Enskog theory¹³ where quantities depend on the binary collision integrals and corresponding interaction potentials. Analytical expressions for collision integrals with Debye-screened coulomb potential are used for charged-charged interactions (see¹⁴). Neutral-neutral and neutral-charged collision integrals are evaluated using tabulated fits from the literature if available (see for example¹⁵) or computed directly by defining a binary interaction potential (in a similar way to¹⁶).

An extended amount of work has been performed on comparing results form the Sethi code to available data in the literature. As an example, we provide in Fig.2 comparisons of thermodynamical (densities, enthalpy and heat capacicty at constant pressure) and transport (electrical conductivity) quantities of an argon mixture with the result of Ref.¹⁷ In general, results show very good agreement with some differences observed in conductivity values. This could be due to different choices in the collision integrals and interaction potentials.

Alkali seeding of the re-entry flow has been suggested in order to dramatically increase the MHD effects around re-entering vehicles.¹⁸ As a rather simple way of modelling seeding in LTE regimes (low altitudes), we have introduced in Sethi the possibility to generate multi-dimensional thermodynamic and transport tables for both TARANIS and CEDRE. Typically, a dataset of cesium-seeded air would be generated using (P,T,Y_{C_s}) tabulated data, the cesium mass fraction Y_{C_s} ranging from 0 to unity and a zero fraction corresponding to pure air. Because seeding is generally not done in a homogeneous way (for example produced by an alkali-doped ablative heat shield), mass diffusion in the LTE regime needs some special treatment. We adopt here the quasi-binary approximation approach in order to compute diffusion coefficients within a two-species model (only two equations of mass conservation 1). With this approach and for earth re-entry for example, the eight air species (O₂, N₂, NO, O, N, NO⁺, O⁺, N⁺) and the two cesium species Cs and Cs⁺ are combined into two "gases" A and B. The problem is then treated as the diffusion of gas B into gas A using the following definition:¹⁹

$$D_{AB} = \frac{\left[\sum_{i=2}^{p} (1+Z_i) x_i\right] \left[\sum_{i=p+1}^{q} (1+Z_i) x_i\right]}{\sum_{i=2}^{p} x_i \sum_{j=p+1}^{q} x_j / D_{ij}}$$
(6)

where Z_i is the charge state of species i, x_i are the molar fractions and D_{ij} are the binary diffusion coefficients calculated from.²⁰ Air gas A corresponds to species from 2 to p and cesium gas B to species from p+1 to q.

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Figure 2: (a) Number densities, (b) enthalpy, (c) heat capacity at constant pressure and (d) electrical conductivity of an argon LTE mixture (Ar, Ar^+ , Ar^{2+} , Ar^{3+} and electrons) obtained with the Sethi code (full lines). For comparisons, dots are from Ref.¹⁷

As an example of a typical plasma LTE composition for a mixture of air and alkali metal, in this case cesium, we show in Fig.3(a) molar fractions temperature dependency (from 300 to 15 kK) for a 10 % seeded air at atmospheric pressure. One can see the expected start of dissociation of O_2 and N_2 molecules for temperatures above ~ 2000 K. Substantial ionization of atomic nitrogen and oxygen starts above ~ 8000-9000 K whereas, due to its very low ionization potential (~ 3.9 eV), cesium starts being ionized at only ~ 2000 K. A direct consequence of the presence of cesium can be observed in Fig.3(b) where electrical conductivity is shown for different cases: pure air, 1, 5 and 20 % Cs-seeded air. We see that when cesium is present, substantial conductivity values are obtained at low temperatures. At high temperatures, conductivity becomes basically independent of cesium fraction.



Figure 3: Results from Sethi: (a) Temperature dependency of molar fractions of an LTE air-cesium mixture at atmospheric pressure(10 % of cesium) (b) Electrical conductivity of different air-cesium mixtures

2.4 Modelling of non-equilibrium flows: a three-temperatures model

The question of identifying the correct regime of the re-entry flow is a complex task. One way of looking at this problem is evaluating the binary scaling parameter $\rho R_n [kg.m^{-2}]$ (R_n is typically the re-entry vehicle nose radius).²¹ As the value of this parameter increases (higher densities/lower altitudes or larger vehicles), we transition from highly non-equilibrium flow (thermal and chemical non-equilibrium) to LTE flows with intermediate regime being thermal

equilibrium but thermal non-equilibrium. For vehicle velocities greater than ~ 5 km/s, transitions occur very roughly at $\rho R_n \approx 10^{-4} kg.m^{-2}$ for full non-equilibrium to intermediate regime and $\rho R_n \approx 10^{-2} kg.m^{-2}$ for intermediate to LTE. In order to model a full trajectory or at least a multi-sampling of a trajectory (with steady state for each chosen point of the trajectory), one need to take into account multi-modes energy distribution over finite timescales. To achieve this, we have implemented a three-temperatures model into the TARANIS code. We therefore keep track, in addition of the total energy, of the vibrational energy energy per unit volume $\rho \mathcal{E}_{\nu}$ and the translational electronic energy per unit volume $\rho \mathcal{E}_{e}$:²²

$$\frac{\partial}{\partial t}(\rho\mathcal{E}_{\nu}) + \nabla \cdot (\rho\mathcal{E}_{\nu}\nu) - \nabla \cdot (\lambda_{\nu}\nabla T_{\nu}) - \nabla \cdot \left(\rho\sum_{s=m}\mathcal{E}_{\nu s}D_{s}\nabla y_{s}\right) = \dot{\Omega}_{\nu}$$
(7)

with

$$\dot{\Omega}_{v} = \dot{\Omega}^{VT} + \dot{\Omega}^{VE} - \dot{\Omega}_{v}^{D}.$$

where the $\dot{\Omega}^{VT}$ term represents the energy exchange between vibrational and translational modes due to collisions, the $\dot{\Omega}^{VE}$ term the energy exchange between vibrational and electronic modes and finally the $\dot{\Omega}_{\nu}^{D}$ term which represents the vibrational energy lost or gained due to molecular dissociation or recombination.

and:

$$\frac{\partial}{\partial t}(\rho\mathcal{E}_e) + \nabla \cdot (\rho\mathcal{E}_e \mathbf{v}) + p_e \nabla \cdot \mathbf{v} - \nabla \cdot (\lambda_e \nabla T_e) - \nabla \cdot (\rho h_e D_e \nabla y_e) = \frac{j^2}{\sigma} + \dot{\Omega}_e \tag{8}$$

with

$$\dot{\Omega}_e = \dot{\Omega}^{ET} - \dot{\Omega}^{VE} - \dot{\Omega}^D_e - \dot{\Omega}^I_e + \dot{\Omega}^C_e,$$

where the $\dot{\Omega}_{e}^{ET}$ term represents the energy exchange between between electrons and heavy particles due to elastic collisions, the $\dot{\Omega}_{e}^{D}$ term the energy loss due to electron impact dissociation, the $\dot{\Omega}_{e}^{I}$ term the energy loss due to electron impact ionization and finally the $\dot{\Omega}_{e}^{C}$ term the energy gain due to electron production. Note here the ohmic heating j^{2}/σ term present as a source term for electron energy.

As total internal energy is the sum of the translational and rotational energy of heavy species, the vibrational energy of molecules and the translational energy of electrons, the translational and rotational energy per unit volume $\rho \mathcal{E}_{tr}$ can be retrieved easily as $\rho \mathcal{E}_{tr} = \rho \mathcal{E} - \rho \mathcal{E}_v + \rho \mathcal{E}_e$. Note here that equilibration between rotational and heavy translational modes is assumed.

Alongside this multi-energy model, a multi-temperature chemistry module has also been implemented into TARANIS with the use of the RADAU method adapted for stiff problems.²³ Arrhenius-type reactions rates are defined using one or a combination of the available three temperatures: electronic T_e , vibrational T_v and heavy-rotational T. The choice depends on the reaction type with for example reactions involving electrons being at the electronic temperature. Forward T_f and T_b backward temperatures used for typical reactions are indicated in Tab. 1. When using the chemistry module, Eq.1 is of course modified by addition of the proper mass source terms in the RHS for each of the species included in the model.

Table 1:	Contro	Jinng	temperatures	s for	various	reaction	mec	manisms
						_		

Reaction	T_{f}	T_b
Ionization by neutral impact	Т	Т
Ionization by electron impact	T_{e}	T_e
Dissociation by neutral impact	$\sqrt{TT_v}$	Т
Dissociation by electron impact	T_{e}	T_{e}
Neutral exchange	Т	Т
Charge exchange	Т	Т
Associative ionization	Т	T_{e}
Reassociation	Т	Т

3. Some examples of applications

3.1 Modelling of laboratory hypersonics experiments in expansion tubes

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A sustained effort to confront and validate theoretical models and numerical tools with experiments is of crucial importance. Experiments aiming at generating and quantifying an MHD effect on a hypersonic flow are typically performed

DOI: 10.13009/EUCASS2023-929

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in high-enthalpy wind tunnels²⁴ (necessary to obtain enough ionization of the flow) or in shock tubes facilities.³ Fine knowledge of the freestream flow properties is usually a delicate question and substantial work is typically needed in order to characterize correctly all relevant parameters. In particular, ionization level of the flow is an important question when dealing with MHD experiments. The group at university of Queensland has in this context produced detailed description of their shock-tube test conditions and have shown in particular that they are able to produce basically nonionized freestream flows. Interestingly, they have performed experiments in argon gas, allowing for easier comparisons with simulations due to simpler thermodynamics and chemical properties. An ongoing work is carried out at ONERA to numerically reproduce their setup. It consists of an either insulated or conductive magnetized sphere of diameter \sim 38 mm (see inset in Fig.4(a)). Looking at specific test conditions, the incoming flow is characterized by T=1112 K, P=427 Pa and v=6306 m/s. Some preliminary results are shown in Fig.4 for magnetic field at sphere surface of ~ 1 T. In Fig.4(a) the electromotive $\mathbf{v} \times \mathbf{B}$ field is visualized with clear observation of the shock discontinuity acting on the velocity. Azimuthal induced electrical currents are obtained by multiplication with the conductivity σ : $\mathbf{j} = \sigma \mathbf{v} \times \mathbf{B}$. To visualize influence of non equilibrium effects, we show in Fig.4(b), (c) and (d) comparisons of temperature, conductivity and Lorentz forces maps obtained for LTE or in chemical nonequilibrium (noted "NE" in the figure). In this regime and because of the small size of the sphere, large differences are observed. Chemical reactions included for non-equilibrium calculations are given below:

$$Ar + Ar \stackrel{k_1}{\underset{k_{-1}}{\leftrightarrow}} Ar^+ + e^- + Ar$$
$$Ar + Ar^+ \stackrel{k_2}{\underset{k_{-2}}{\leftrightarrow}} Ar^+ + e^- + Ar^+$$
$$Ar + e^- \stackrel{k_3}{\underset{k_{-3}}{\leftrightarrow}} Ar^+ + e^- + e^-$$

with forward and backward arrows indicating direct and reverse reactions. The reaction rates k_i are estimated using Arrhenius-type expression $AT^B e^{T/T_a}$ with values of A, B and T_a coefficients deduced from Queensland work:

- $k_1 : A = 0.1045 \ m^3.mol^{-1}.s^{-1}, B = 1.418, T_a = 101500 \ K$
- $k_2: A = 0.1045 \ m^3.mol^{-1}.s^{-1}, B = 1.418, T_a = 101500 \ K$
- $k_3: A = 976.8 \ m^3.mol^{-1}.s^{-1}, B = 1.418, T_a = 101500 \ K$

Reverse rates are deduced from the forward rates using the equilibrium constant.

Kinetic energy of the incoming flow is in one case (LTE) converted instantaneously in thermal and chemical reactions whereas when finite-rate chemical reactions are allowed most of the energy is converted solely into kinetic (translational) energy. This explains the large differences in temperatures observed in Fig.4(b). Because ionizing reactions do not have time to proceed, ionization degree and resulting electrical conductivity is much smaller in the non-equilibrium case (see Fig.4(c)). As a consequence, Lorentz forces are also of lower magnitudes in the non-equilibrium case, Fig.4(d). Despite the higher values of magnetic forces in the LTE case, the shock-to-nose distance is smaller in this case (see Fig.4(b)). This is because the hotter post-shock plasma in the non-equilibrium case is of lower mass density and therefore steady-state implies a thicker layer of the shocked flow. Work is underway to include multi-temperature effects to these simulations.

3.2 Modelling of martian re-entry

Here we present numerical results from the highly non-equilibrium conditions of martian re-entry. Because of atmospheric pressure ~ 100 times lower than in earth atmosphere, most if not all of the re-entry trajectory can actually be considered as being in a non-equilibrium regime. We make use of the previously described three-temperatures model to investigate the mars re-entry of a pathfinder-type geometry.²⁶ A magnetic dipole is placed near the nose of the vehicle as it can be seen in Fig.5(a) where colormap corresponds to B-field magnitude (0.3 T at maximum on vehicle surface) and black lines correspond to the streamlines of the dipolar magnetic field. Some results from our 2D axisymmetric simulations are shown in Fig.5(b) with on top the molar fraction of electrons and bottom the electrical conductivity. Freestream conditions here correspond to a velocity of 6.5 km/s and a martian altitude of 50 km. Maximum fraction of electron is ~ 4.10^4 close to the nose, a relatively small value mostly due to chemical non-equilibrium. Maximum value of conductivity is ~ 120 S/m also in the post-shoc region close to the nose. In the 2D map of Fig.5(c) we show colormap of the electron temperature. A first lineout is taken along the stagnation line (top curves) where clear evidence of energy decoupling is observed in a small region close to the shock itself. Because most of the initial kinetic energy is carried

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Figure 4: Numerical results on the Queensland's laboratory setup shown as inset in (a) (taken from²⁵). (a) Electromotive field $\mathbf{v} \times \mathbf{B}$ and temperature and zoom on (b) temperature (c) electrical conductivity (d) and Lorentz force magnitude are displayed for both the LTE and the chemically non-equilibrium regimes ("NE"). Flow is always from left to right.

out by the heavy particles, it is the associated temperature T (red curve) that is maximum at the shock with a peak at $\sim 16\ 000\ K$. Electronic and vibrational temperatures are $\sim 7000-8000\ K$, roughly two times smaller. Now looking at temperatures downstream, we observe a relatively spread region where substantially hotter electrons are present. A lineout across this region (bottom right image) show that there electron temperature is $\sim 12\ 000\ K$ whereas vibrational and heavy temperature is roughly two times lower at $\sim 6000-7000\ K$. We attribute this effect to the localized strong ohmic heating of the electron population (it is in this region that the flow has maximum $\mathbf{v} \times \mathbf{B}$ value). These result could be of importance for MHD effects since in particular the electrical conductivity depends solely on the electron temperature. These preliminary results which are yet to be studied in detail tend to show strong non-homogeneous and non-equilibrium effects associated to the presence of the magnetic field. Further investigation is needed to clarify the complete picture about these mechanisms, in particular their dependency to freestream conditions.

3.3 Hall effect in re-entry flows

As a last example, we quickly present the effect of an extended MHD mechanism, namely the Hall effect. It can be included in our model by modification of the definition of the Ohm's law. Indeed if we now write:

 $j = \widetilde{\sigma} \cdot (E + v \times B) \tag{9}$

with

$$\widetilde{\boldsymbol{\sigma}} = \begin{pmatrix} \sigma_P & \sigma_H & \sigma_P \\ \sigma_H & \sigma_P & 0 \\ 0 & 0 & \sigma_e \end{pmatrix}.$$

 $\sigma_e = \frac{n_e q_e^2}{m_e v_e}.$

 $\sigma_H = \frac{\beta_e}{1 + \beta_e^2} \sigma_e$

 $\sigma_P = \frac{1}{1 + \beta_e^2} \sigma_e.$

and,

we now have have a tensorial expression of the electrical conductivity.
$$\sigma_e$$
 is the "standard" conductivity used in
the resistive Ohm's law 5. σ_H and σ_P are respectively called the Hall and the Pedersen conductivities. β_e is the electron
Hall parameter defined as

$$\beta_e = \frac{\omega_c}{\nu_e}$$

DOI: 10.13009/EUCASS2023-929

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Figure 5: Simulation of mars pathfinder-type re-entry vehicle in martian atmospheric conditions (50 km, 6.5 km/s). (a) Colormap of magnetic field magnitude and streamlines of magnetic field (b) top half: electron molar fraction bottom half: electrical conductivity (c) left: colormap of electronic temperature and right: lineouts at different positions of the electornic temperature. FLow is always from left to right.

with the electron cyclotron frequency $\omega_c = |q_e| B/m_e$ and v_e the total electron collision frequency. For sake of simplicity, when deriving expression for the generalized Ohm's law 9, it was assumed that B-field was along z-direction. From this new expression, we can see that the current will in general not be aligned with the effective electric field $E + v \times B$. It will however be a very good approximation when β_e approaches zero, that is for non-magnetized electrons. This effect has been implemented in TARANIS and a visual demonstration of one of its consequences on MHD re-entry is shown in Fig.6. Here we show on the left the distribution of Hall parameter for an magnetized (1 T on vehicle surface) axisymmetric hemispheric re-entry geometry in earth atmosphere at 6.5 km/s and an altitude of 60 km. For this high altitude/low density regime, collisions are weak enough to make Hall parameters much larger than one, making

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tensorial conductivity expressed in Eq.9 relevant. Without Hall effect it is expected to observe from this configuration only out-of-plane electrical currents because magnetic moment is oriented in the plane, along the top symmetry axis. Now if we look at the right image in Fig.6, in-plane "Hall" currents are clearly circulating around the vehicle in the conductive post-shock plasma. We note here that the vehicle body is considered in our simulation as an insulator and therefore current forms closed loop in the plasma. A well known consequence of the circulation of these Hall currents is a potentially strong deterioration of the primary desired MHD effect involving flow deceleration through azimuthal electrical currents induced in the $\mathbf{v} \times \mathbf{B}$ direction.²⁷



Figure 6: Hall effect on a simple 2D axisymmetric hemispherical geometry in earth atmosphere. The flow is from the left to the right with freestream condition corresponding to v=6.5 km/s and 60 km altitude. On left image is represented the Hall parameter whereas on the right image current streamlines of the in-plane "Hall" currents are shown.

4. Conclusion

MHD techniques could bring novel solutions to the problems of heating and trajectory control for space vehicles reentry. We develop at ONERA an extended suit of numerical tools with the aim of capturing the physical mechanisms at work when a magnetic field is applied to the post-shock ionized flow.

The problem is treated by coupling the ONERA's CEDRE platform to our in-house MHD code TARANIS. We are able to model complex geometries with multi-materials both for the fluid and the electromagnetism. Electric potential is solved alongside fluid quantities. For an interaction parameter high enough, strong modification of the flow is possible. It is then possible to consider efficient MHD mitigation of heat transfert from the flow to the vehicle as well as the modification of the aerodynamic coefficients. Future works include the improvement of our numerical tools with the capability to model self-consistently the seeded heat shield ablation, turbulent effects... We also aim to validate our codes and models with MHD experiments on ONERA and/or academic wind tunnels or shock tubes.

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